

## 7-1 Worksheet: Basic Trig Identities

Use the given information to determine the exact trigonometric value if  $0^\circ < \theta < 90^\circ$

1).  $\cos \theta = \frac{1}{4}$ , find  $\tan \theta$

2). If  $\sin \theta = \frac{2}{3}$ , find  $\cos \theta$

3). If  $\tan \theta = \frac{7}{2}$ , find  $\sin \theta$

4). If  $\tan \theta = 2$ , find  $\cot \theta$

*Express each value as a trigonometric function of an angle in Quadrant I.*

5).  $\cos 892^\circ$

6).  $\csc 495^\circ$

7).  $\sin \frac{23\pi}{3}$

*Simplify each expression.*

8).  $\cos x + \sin x \tan x$

9).  $\frac{\cot A}{\tan A}$

## 7-2 Worksheet: Proving Trig Identities

*Verify that each equation is an identity and state the domain of the identity.*

$$1). \frac{\csc x}{\cot x + \tan x} = \cos x$$

$$2). \frac{1}{\sin x - 1} - \frac{1}{\sin x + 1} = -2\sec^2 x$$

$$3). \sin^3 x - \cos^3 x = (1 + \sin x \cos x)(\sin x - \cos x)$$

$$4). \tan x + \frac{\cos x}{1 + \sin x} = \sec x$$

*Find a numerical value of one trigonometric function of  $x$ .*

$$5). \sin x \cot x = 1$$

$$6). \sin x = 3 \cos x$$

$$7). \cos x = \cot x$$

## 7-3 Worksheet: Sum and Difference Identities

*Use the sum and difference identities to find the exact value of each trig function.*

1).  $\cos \frac{5\pi}{12}$

2).  $\sin(-165^\circ)$

3).  $\tan\left(-\frac{7\pi}{12}\right)$

4).  $\sec \frac{\pi}{12}$

**Find each exact value if  $0 < y < \frac{\pi}{2}$ ,  $\frac{\pi}{2} < x < \pi$**

5).  $\cos(x + y)$  if  $\sin x = \frac{3}{5}$ ,  $\sin y = \frac{2}{7}$

6).  $\sin(x - y)$  if  $\cos x = -\frac{8}{17}$  and  $\cos y = \frac{3}{5}$

**Verify that each equation is an identity.**

7).  $\cos(180^\circ - \theta) = -\cos \theta$

8).  $\sin(360^\circ + \theta) = \sin \theta$

## 7-4 Worksheet: Double-Angle Identities

*Use the given information to find  $\sin 2x$ ,  $\cos 2x$*

1).  $\sin x = \frac{12}{13}$ , for  $0 < x < 90$

2).  $\sec x = -\frac{5}{2}$ , for  $\frac{\pi}{2} < x < \pi$

*Use the given information to find  $\sin 2x$ ,  $\cos 2x$*

3).  $\sin x = \frac{3}{5}$ , for  $0 < x < \frac{\pi}{2}$

*Verify that each equation is an identity.*

4).  $1 + \sin 2x = (\sin x + \cos x)^2$

5).  $\cos x \sin x = \frac{\sin 2x}{2}$



## 7-5 Worksheet: Solving Trigonometric Equations

*Solve each equation for principal values of  $x$ . Express solutions in degrees.*

1).  $\cos x = 3 \cos x - 2$

2).  $2 \sin^2 x - 1 = 0$

*Solve each equation for  $0 \leq x < 360$*

3).  $\sin^2 x - 2 \sin x + 1 = 0$

4).  $\cos 2x + 3 \cos x - 1 = 0$

*Solve each equation for  $0 \leq x < 2\pi$*

5).  $4\sin^2 x - 4\sin x + 1 = 0$

6).  $\cos 2x + \sin x = 1$

*Solve each equation for all real values of  $x$ .*

7).  $3\cos 2x - 5\cos x = 1$

8).  $2\sin^2 x - 5\sin x + 2 = 0$

9).  $3\sec^2 x - 4 = 0$

10).  $\tan x(\tan x - 1) = 0$

# Advanced Math

Name \_\_\_\_\_

## Chapter 7 review Part 1

1. Given  $\frac{3\pi}{2} \leq x \leq 2\pi$  and  $\cos x = \frac{5}{8}$  find the following:

a.  $\sin x =$

b.  $\csc x =$

c.  $\tan x =$

d.  $\sec x =$

e.  $\cot x =$

2. Given  $90^\circ \leq x \leq 180^\circ$  and  $\tan x = \frac{-5}{3}$  find the following:

a.  $\cos 2x =$

b.  $\sin 2x =$

3. Given:  $\frac{\pi}{2} \leq x \leq \pi$  and  $\sin x = \frac{1}{5}$ . Given:  $\frac{3\pi}{2} \leq y \leq 2\pi$  and  $\cos y = \frac{6}{7}$ .

a. Find  $\cos(x - y)$

b. Find  $\sin(x + y)$

4. Find  $\sin(255^\circ)$

5. Find  $\cos\left(\frac{7\pi}{12}\right)$

6. Find  $\cos\left(\frac{3\pi}{8}\right)$

7.  $\sin(105^\circ)$

8.  $\sin\left(\frac{\pi}{12}\right)$  **SKIP**

## Advanced Math

### Chapter 7 review Part 2

Solve each equation for principal values of  $x$ .

1.  $2 \sin x + 1 = 0$

2.  $2 \cos^2 x + 3 \cos x = 2$

Solve each equation for the interval  $0 \leq x \leq 2\pi$ .

3.  $4 \sin^2 x + 1 = -4 \sin x$

4.  $\cos x \tan x - 2 \cos^2 x = -1$

Solve each equation where the Domain of  $x$  is all real #'s.

5.  $3 \cos^2 x = 6 \cos x - 3$

6.  $4 \sin^2 x - 2 = 0$

Verify that the following trigonometric expressions are identities. State the domain restrictions if any.

$$1. \frac{\cos x}{\sec x} + \frac{\sin x}{\csc x} = \sec^2 x - \tan^2 x$$

Domain:

$$2. \frac{1}{1-\cos x} + \frac{1}{1+\cos x} = 2 \csc^2 x$$

Domain:

$$3. \frac{\sin q}{\csc q} + \frac{\cos q}{\sec q} = \sin q \csc q$$

Domain:

$$4. \frac{\tan^2 q}{1 + \tan^2 q} = \sin^2 q$$

Domain:



Solve the following inequalities. Domain  $0 \leq x \leq 2\pi$ . Hint... Draw the circle and the cosine or sine wave 😊.

1.  $\cos x \leq \frac{-\sqrt{3}}{2}$

2.  $\cos x - \frac{1}{2} > 0$

3.  $\sqrt{2} \sin x - 1 < 0$