Name_

Evaluate each expression.



Simplify each expression.

7.
$$(5n^3)^2 \cdot n^{-6}$$
 8. $\left(\frac{x^2}{4y^{-2}}\right)^{-\frac{1}{2}}$ 9. $(64x^6)^{\frac{1}{3}}$

10.
$$(5x^6y^4)^{\frac{1}{2}}$$
 11. $\sqrt{x^2y^3} \cdot \sqrt{x^3y^4}$ **12.** $\left(\frac{p^{6a}}{p^{-3a}}\right)^{\frac{1}{3}}$

Express each using rational exponents.

13.
$$\sqrt{x^5 y^6}$$
 14. $\sqrt[5]{27x^{10}y^5}$
 15. $\sqrt{144x^6 y^{10}}$

 16. $21\sqrt[3]{c^7}$
 17. $\sqrt{1024a^3}$
 18. $\sqrt[4]{36a^8b^5}$
Express each using radicals.
 19. $64^{\frac{1}{3}}$
 20. $2^{\frac{1}{2}}a^{\frac{3}{2}}b^{\frac{5}{2}}$
 21. $s^{\frac{2}{3}}t^{\frac{1}{3}}v^{\frac{2}{3}}$

 22. $y^{\frac{3}{2}}$
 23. $x^{\frac{2}{5}}y^{\frac{3}{5}}$
 24. $(x^6y^3)^{\frac{1}{2}}z^{\frac{2}{3}}$

Logarithmic Functions

Write each equation in exponential form.

1.
$$\log_3 81 = 4$$

2. $\log_8 2 = \frac{1}{3}$
3. $\log_{10} \frac{1}{100} = -2$

Write each equation in logarithmic form.

4.
$$3^3 = 27$$
 5. $5^{-3} = \frac{1}{125}$ 6. $\left(\frac{1}{4}\right)^{-4} = 256$

Evaluate each expression.

7. $\log_7 7^3$	8. $\log_{10} 0.001$	9. log ₈ 4096

10.	\log_4	32
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11. log₃1

12. $\log_6 \frac{1}{216}$

Solve each equation.

13. $\log_x 64 = 3$

14. $\log_4 0.25 = x$

15. $\log_4(2x-1) = \log_4 16$

16. $\log_{10} \sqrt{10} = x$

17. $\log_7 56 - \log_7 x = \log_7 4$

18. $\log_5(x+4) + \log_5 x = \log_5 12$

Name_

Graph each exponential function or inequality.







3. $y > -3^x + 1$



4. $y \ge 0.5^x$



5. $y \ge \log_3(x+2)$



1. *Demographics* An area in North Carolina known as The Triangle is principally composed of the cities of Durham, Raleigh, and Chapel Hill. The Triangle had a population of 700,000 in 1990. The average yearly rate of growth is 5.9%. Find the projected population for 2010.

2. *Finance* Determine the amount of money in a savings account that provides an annual rate of 4% compounded monthly if the initial investment is \$1000 and the money is left in the account for 5 years.

3. *Investments* How much money must be invested by Mr. Kaufman if he wants to have \$20,000 in his account after 15 years? He can earn 5% compounded quarterly.

4. **Chemistry** How long would it take 100,000 grams of radioactive iodine, which has a half-life of 60 days, to decay to 25,000 grams? Use the formula $N = N_0 \left(\frac{1}{2}\right)^t$, where N is the final amount of the substance, N_0 is the initial amount, and t represents the number of half-lives.

Name_____

Given that log 3 = 0.4771, log 5 = 0.6990, and log 9 = 0.9542, evaluate each log.

1. log 300,000	2. log 9000	3. log 75
4. log 0.0005	5. log 27	6. log 81
Evaluate each expression.		
7. log 66.3		9. log 7(4³)

Find the value of each logarithm using the change of base formula.

10. log₆ 832

11. log₁₁ 47

12. log₃ 9

Solve each equation or inequality.

13. $8^{x} = 10$	14. $1.8^{x-5} = 19.8$	15. 4 ^{2x} > 25

16. 2.4[×] ≤ 20

17. 3^{5x} = 85

18. $3^{2x-2} = 2^x$

1. In 1995, the population of Kalamazoo, MI, was 79, 089. This figure represented a 0.4% annual decline from 1990.

- a. Let *t* be the number of years since 1995 and write a function that models the population in Kalamazoo in 1995.
- b. Predict the population in 2010 and in 2015. Assume a steady rate of decline.
- 2. Suppose Karen deposits \$1500 in a savings account that earns 6.75% interest compounded continuously. She plans to withdraw the money in 6 years to make a \$2500 down payment on a car. Will there be enough funds for Karen to meet her goal?

- 3. Given the original principal, the annual interest rate, the amount of time for each investment, and the type of compounded interest, find the amount of each account.
 - a. P = \$1250, r = 8.5%, t = 3 years, semiannually.
 - b. P = \$2575, r = 6.25%, t = 5 years 3 months, continuously.

Evaluate each expression.

4. ln 71

5. ln 8.76

6. ln 0.532

7. log ₄ 94

8. log ₅ 256

9. log ₉0.712

Use natural logs to solve each equation.

10. 6[×] = 42

11. $7^{x} = 4^{x+3}$

12. 1249 = 175e^{-0.04t}

Exponential Extras

1. Graph the exponential functions $y = 3^x$, $y = 3^x + 5$, and $y = 3^x - 4$ on the same set of axes. In complete sentences, compare and contrast the graphs. *LABEL EACH*



2. Between 1990 and 2000, the population of Florida had an annual growth rate of about 2.14%. If the state's population was 15,989,069 in 2000, approximately what was Florida's population in 1990?

3. Determine the amount of money in a savings account providing an annual rate of 3% compounded daily if Sandra made a one-time deposit of \$8500 in to the account and left it there for 5 years.

4. Graph $y > 3^{x} - 2$.



- 5. Jared purchases a new car for \$26,400. The car loses 21.5% of its value each year.
- a. Write a function to model the VALUE of the car.
- b. Find the value of the car after 4 months of ownership
- c. Find the value of the car after three years of ownership.
- d. Graph the function and use the graph to verify your answer in part b.



6. Compare the balance after 15 years of a \$20,000 investment earning 7% interest compounded continuously to the same investment compounded quarterly.

7. Write each equation in exponential form.

a.
$$\log_{32} 8 = \frac{3}{5}$$
 b. $\log_{81} 3 = \frac{1}{4}$

8. Write each equation in logarithmic form.

a.
$$6^4 = 1296$$
 b. $2^{-8} = \frac{1}{256}$

9. Evaluate the expression
$$\log_3 \frac{1}{27}$$

10. Given that log 4 = 0.6021, evaluate the logarithm: log 40,000

11. Evaluate each expression.

a. log 4(3)⁴

b.
$$\log \frac{22^3}{4}$$

12. Graph $y < \log(x + 2)$.



13. Find the value of $\log_8 550$ using the change of base formula.

14. Convert $\log_4 325$ to a natural logarithm and evaluate.

15. Solve 6.7 = -8.2 ln *x*.

16. Solve the equation by using natural logarithms: $4^{3x} = 5^{x-8}$